

Name \_\_\_\_\_

**Subtract the polynomials.**

1)  $(6x^5 + 16x^2 + 6) - (-12x^2 + 2x^5 - 9)$

1) \_\_\_\_\_

2)  $(8x^5 - 14x^2 - 10) - (16x^2 + 5x^5 + 6)$

2) \_\_\_\_\_

3)  $(5x^3 + 2x^5 + 5 + 9x^4) - (-6 + 2x^4 + 9x^5 - 3x^3)$

3) \_\_\_\_\_

4)  $(8x^2 + 5x^4 - 4 + 2x^3) - (1 + 7x^3 + 7x^4 + 2x^2)$

4) \_\_\_\_\_

**Find the product.**

5)  $\left( -\frac{1}{2}x - 7 \right) \left( \frac{1}{5}x + 6 \right)$

5) \_\_\_\_\_

6)  $\left( \frac{1}{3}x + 10 \right) \left( \frac{1}{3}x + 11 \right)$

6) \_\_\_\_\_

7)  $(x - 5)(x^2 + 5x - 2)$

7) \_\_\_\_\_

8)  $(9x - 1)(x^2 - 4x + 1)$

8) \_\_\_\_\_

**Factor completely using the grouping method to factor trinomials. If unfactorable, indicate that the polynomial is prime.**

9)  $5x^2 + 56x + 11$

9) \_\_\_\_\_

10)  $2x^2 + 23x + 11$

10) \_\_\_\_\_

11)  $3x^2 + 13x + 10$

11) \_\_\_\_\_

12)  $3x^2 - 7x - 6$

12) \_\_\_\_\_

13)  $2x^2 + 11x + 12$

13) \_\_\_\_\_

14)  $3x^2 + 19x + 10$

14) \_\_\_\_\_

15)  $2x^2 - 11x + 15$

15) \_\_\_\_\_

**Factor completely.**

16)  $8p^3 - 1$

16) \_\_\_\_\_

17)  $64p^3 - 1$

17) \_\_\_\_\_

$18) 343p^3 - 1$       18) \_\_\_\_\_

$19) x^3 - 1000$       19) \_\_\_\_\_

$20) x^3 - 729$       20) \_\_\_\_\_

$21) x^3 - 125$       21) \_\_\_\_\_

$22) t^3 + 1000$       22) \_\_\_\_\_

$23) t^3 + 8$       23) \_\_\_\_\_

$24) t^3 + 125$       24) \_\_\_\_\_

$25) a^3b^3 + 64$       25) \_\_\_\_\_

$26) a^3b^3 + 8$       26) \_\_\_\_\_

**Solve. Round to two decimal places unless otherwise noted.**

27) If the average cost per unit  $C(x)$  to produce  $x$  units of plywood is given by  $C(x) = \frac{900}{x + 30}$ , 27) \_\_\_\_\_

what is the unit cost for 50 units?

28) If the average cost per unit  $C(x)$  to produce  $x$  units of plywood is given by  $C(x) = \frac{1200}{x + 40}$ , 28) \_\_\_\_\_

what is the unit cost for 50 units?

29) Suppose the cost per ton,  $C(x)$ , to build an oil platform of  $x$  thousand tons is approximated 29) \_\_\_\_\_  
by  $C(x) = \frac{262,500}{x + 525}$ . What is the cost per ton for 50 thousand tons?

30) Suppose the cost per ton,  $C(x)$ , to build an oil platform of  $x$  thousand tons is approximated 30) \_\_\_\_\_  
by  $C(x) = \frac{262,500}{x + 525}$ . What is the cost per ton for 10 thousand tons?

31) In the following formula,  $S(x)$  is the minimum number of hours of studying required to attain 31) \_\_\_\_\_  
test score of  $x$ :

$$S(x) = \frac{0.49x}{100.5 - x}.$$

How many hours of study are needed to score 90?

32) In the following formula,  $S(x)$  is the minimum number of hours of studying required to attain 32) \_\_\_\_\_  
test score of  $x$ :

$$S(x) = \frac{0.43x}{100.5 - x}.$$

How many hours of study are needed to score 85?

**Simplify by factoring.**

$$33) \frac{3x + 12}{x^2 + 4x}$$

$$33) \underline{\hspace{2cm}}$$

$$34) \frac{4x + 16}{x^2 + 4x}$$

$$34) \underline{\hspace{2cm}}$$

$$35) \frac{3x + 4}{15x^2 + 26x + 8}$$

$$35) \underline{\hspace{2cm}}$$

$$36) \frac{3x + 2}{15x^2 + 22x + 8}$$

$$36) \underline{\hspace{2cm}}$$

$$37) \frac{y^2 + 10y + 21}{y^2 + 11y + 24}$$

$$37) \underline{\hspace{2cm}}$$

$$38) \frac{y^2 - 3y - 10}{y^2 + 2y - 35}$$

$$38) \underline{\hspace{2cm}}$$

$$39) \frac{m^2 - 25}{m^2 - 10m + 25}$$

$$39) \underline{\hspace{2cm}}$$

$$40) \frac{m^2 - 64}{m^2 + 16m + 64}$$

$$40) \underline{\hspace{2cm}}$$

List all numbers for which the rational expression is undefined.

$$41) \frac{b - 7}{7b - 21}$$

$$41) \underline{\hspace{2cm}}$$

$$42) \frac{b - 8}{8b - 16}$$

$$42) \underline{\hspace{2cm}}$$

$$43) \frac{x^2 - 25}{x^2 + 15x + 56}$$

$$43) \underline{\hspace{2cm}}$$

$$44) \frac{x^2 - 49}{x^2 + 13x + 40}$$

$$44) \underline{\hspace{2cm}}$$

$$45) \frac{x^2 - 36}{x^2 - 13x + 42}$$

$$45) \underline{\hspace{2cm}}$$

$$46) \frac{x^2 - 49}{x^2 + 4x - 32}$$

$$46) \underline{\hspace{2cm}}$$

$$47) \frac{x^2 - 25}{x^2 - 7x - 18}$$

$$47) \underline{\hspace{2cm}}$$

**MULTIPLE CHOICE.**

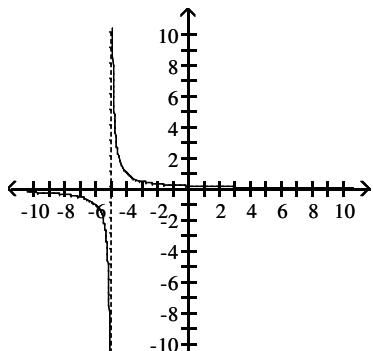
Choose the one alternative that best completes the statement or answers the question.

Show all work in the space provided.

Choose the correct equation of the given graph.

48)

48) \_\_\_\_\_



A)  $f(x) = \frac{x+5}{x}$

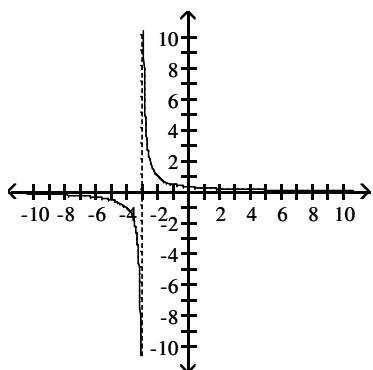
B)  $f(x) = \frac{x}{x+5}$

C)  $f(x) = \frac{1}{x-5}$

D)  $f(x) = \frac{1}{x+5}$

49)

49) \_\_\_\_\_



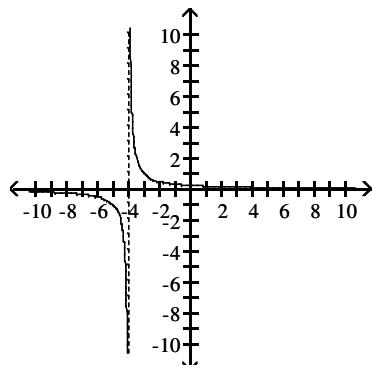
A)  $f(x) = \frac{x+3}{x}$

B)  $f(x) = \frac{1}{x+3}$

C)  $f(x) = \frac{x}{x+3}$

D)  $f(x) = \frac{1}{x-3}$

50)



A)  $f(x) = \frac{1}{x+4}$

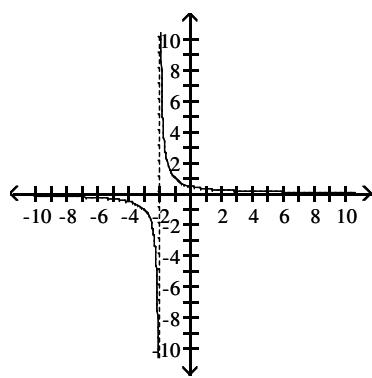
B)  $f(x) = \frac{x+4}{x}$

C)  $f(x) = \frac{x}{x+4}$

D)  $f(x) = \frac{1}{x-4}$

50) \_\_\_\_\_

51)



A)  $f(x) = \frac{x+2}{x}$

B)  $f(x) = \frac{1}{x-2}$

C)  $f(x) = \frac{1}{x+2}$

D)  $f(x) = \frac{x}{x+2}$

51) \_\_\_\_\_

**Solve the rational equation.**

52)  $\frac{6}{x} + x = \frac{70}{x}$

52) \_\_\_\_\_

53)  $\frac{9}{x} + x = \frac{13}{x}$

53) \_\_\_\_\_

$$54) \frac{x^2 + 2}{x} = \frac{6}{x}$$

54) \_\_\_\_\_

$$55) \frac{x^2 + 3}{x} = \frac{19}{x}$$

55) \_\_\_\_\_

$$56) \frac{x^2 - 9}{9x} = -\frac{5}{9x}$$

56) \_\_\_\_\_

$$57) \frac{x^2 - 14}{8x} = -\frac{5}{8x}$$

57) \_\_\_\_\_

$$58) \frac{x^2 - 14}{4x} = -\frac{5}{4x}$$

58) \_\_\_\_\_

$$59) \frac{1}{x - 4} = \frac{8}{x^2 - 16}$$

59) \_\_\_\_\_

$$60) \frac{1}{x - 1} = \frac{2}{x^2 - 1}$$

60) \_\_\_\_\_

$$61) \frac{1}{x - 9} = \frac{18}{x^2 - 81}$$

61) \_\_\_\_\_

**Solve. Section 5.6A NUMBER PROBLEMS.**

62) The sum of a number and 81 times its reciprocal is 18. Find the number.

62) \_\_\_\_\_

63) The sum of a number and 9 times its reciprocal is 6. Find the number.

63) \_\_\_\_\_

64) The sum of a number and 12 times its reciprocal is 8. Find the number(s).

64) \_\_\_\_\_

65) The sum of a number and 6 times its reciprocal is 7. Find the number(s).

65) \_\_\_\_\_

66) The sum of a number and 5 times its reciprocal is 6. Find the number(s).

66) \_\_\_\_\_

**Solve. Section 5.6A. The time is equal for these and the distance is given. Wind speed is unknown.**

67) A plane flies 490 miles with the wind and 350 miles against the wind in the same length of time. If the speed of the wind is 20 mph, what is the speed of the plane in still air?

67) \_\_\_\_\_

68) A plane flies 440 miles with the wind and 340 miles against the wind in the same length of time. If the speed of the wind is 30 mph, what is the speed of the plane in still air?

68) \_\_\_\_\_

69) A plane flies 500 miles with the wind and 340 miles against the wind in the same length of time. If the speed of the wind is 24 mph, what is the speed of the plane in still air?

69) \_\_\_\_\_

70) A plane flies 440 miles with the wind and 320 miles against the wind in the same length of time. If the speed of the wind is 27 mph, what is the speed of the plane in still air?

70) \_\_\_\_\_

**Solve the problem.**

71) Given  $f(x) = \frac{x+9}{x-4}$  and  $g(x) = \frac{x+9}{x-7}$ , find  $f(x) - g(x)$ .

71) \_\_\_\_\_

72) Given  $f(x) = \frac{x-7}{x-1}$  and  $g(x) = \frac{x-7}{x+9}$ , find  $f(x) - g(x)$ .

72) \_\_\_\_\_

73) Given  $f(x) = \frac{x+3}{x+5}$  and  $g(x) = \frac{x+3}{x-1}$ , find  $f(x) - g(x)$ .

73) \_\_\_\_\_

74) Given  $f(x) = \frac{x-2}{x+8}$  and  $g(x) = \frac{x-2}{x-5}$ , find  $f(x) - g(x)$ .

74) \_\_\_\_\_

75) Given  $f(x) = \frac{8}{3x-21}$  and  $g(x) = \frac{x}{x^2-49}$ , find  $f(x) + g(x)$ .

75) \_\_\_\_\_

76) Given  $f(x) = \frac{3}{4x-32}$  and  $g(x) = \frac{x}{x^2-64}$ , find  $f(x) + g(x)$ .

76) \_\_\_\_\_

77) Given  $f(x) = \frac{10}{3x-6}$  and  $g(x) = \frac{x}{x^2-4}$ , find  $f(x) + g(x)$ .

77) \_\_\_\_\_

78) Given  $f(x) = \frac{7}{4x-8}$  and  $g(x) = \frac{x}{x^2-4}$ , find  $f(x) + g(x)$ .

78) \_\_\_\_\_

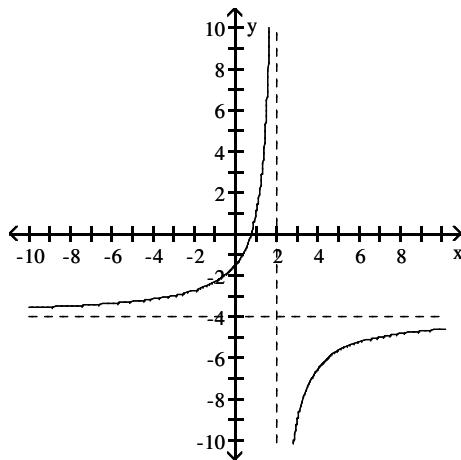
**Find the specified quotient function.**

- 79) Given the functions  $f(x) = x^2 - 3x - 10$  and  $g(x) = x^2 - 5x - 14$ , find an equation of the quotient function  $\frac{f}{g}$ .      79) \_\_\_\_\_
- 80) Given the functions  $f(x) = x^2 + 2x - 24$  and  $g(x) = x^2 - 2x - 48$ , find an equation of the quotient function  $\frac{f}{g}$ .      80) \_\_\_\_\_
- 81) Given the functions  $f(x) = x^2 - 5x - 24$  and  $g(x) = x^2 - 6x - 27$ , find an equation of the quotient function  $\frac{f}{g}$ .      81) \_\_\_\_\_
- 82) Given the functions  $f(x) = x^2 - 16$  and  $g(x) = x^2 - 13x + 36$ , find an equation of the quotient function  $\frac{f}{g}$ .      82) \_\_\_\_\_
- 83) Given the functions  $f(x) = x^2 - 16$  and  $g(x) = x^2 + 3x - 28$ , find an equation of the quotient function  $\frac{f}{g}$ .      83) \_\_\_\_\_

Identify any vertical or horizontal asymptotes in the graph of  $y = f(x)$ . State the domain of  $f$ .

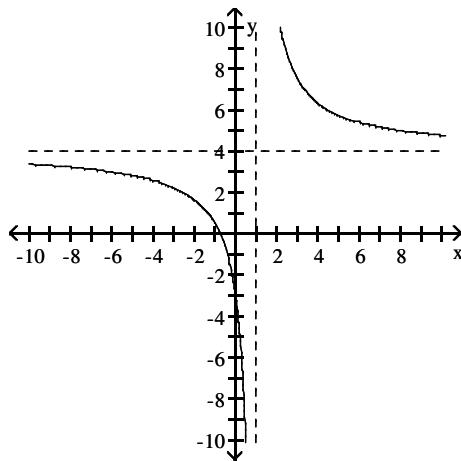
84)

84) \_\_\_\_\_

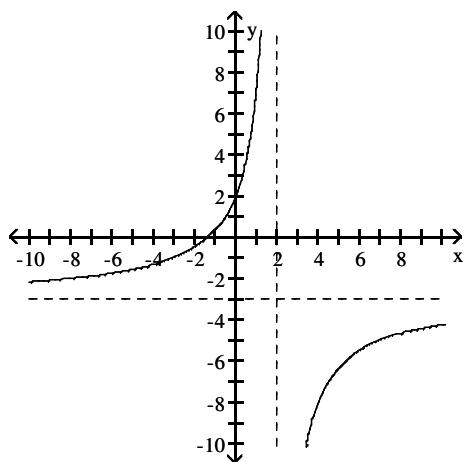


85)

85) \_\_\_\_\_

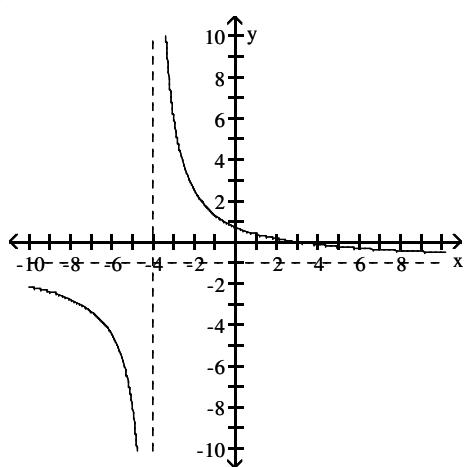


86)



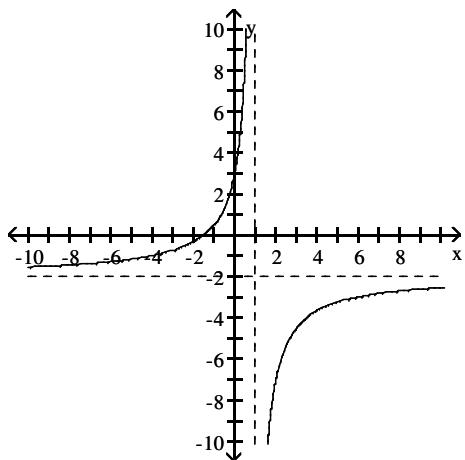
86) \_\_\_\_\_

87)



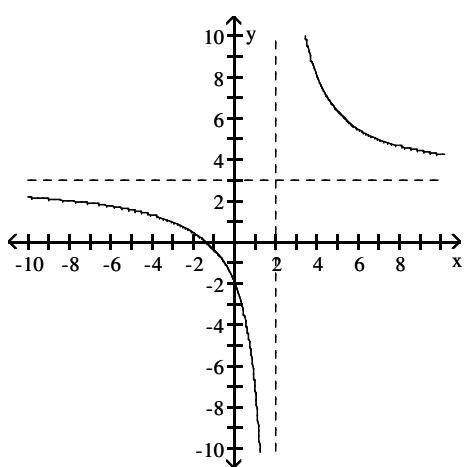
87) \_\_\_\_\_

88)



88) \_\_\_\_\_

89)



89) \_\_\_\_\_

## Answer Key

Testname: EXAM2PREP\_COMPRESSED\_CH4ANDCH5V01

1)  $4x^5 + 28x^2 + 15$

2)  $3x^5 - 30x^2 - 16$

3)  $-7x^5 + 7x^4 + 8x^3 + 11$

4)  $-2x^4 - 5x^3 + 6x^2 - 5$

5)  $-\frac{1}{10}x^2 - \frac{22}{5}x - 42$

6)  $\frac{1}{9}x^2 + 7x + 110$

7)  $x^3 - 27x + 10$

8)  $9x^3 - 37x^2 + 13x - 1$

9)  $(5x + 1)(x + 11)$

10)  $(2x + 1)(x + 11)$

11) prime

12)  $(3x + 2)(x - 3)$

13)  $(2x + 3)(x + 4)$

14) prime

15) prime

16)  $(2p - 1)(4p^2 + 2p + 1)$

17)  $(4p - 1)(16p^2 + 4p + 1)$

18)  $(7p - 1)(49p^2 + 7p + 1)$

19)  $(x - 10)(x^2 + 10x + 100)$

20)  $(x - 9)(x^2 + 9x + 81)$

21)  $(x - 5)(x^2 + 5x + 25)$

22)  $(t + 10)(t^2 - 10t + 100)$

23)  $(t + 2)(t^2 - 2t + 4)$

24)  $(t + 5)(t^2 - 5t + 25)$

25)  $(ab + 4)(a^2b^2 - 4ab + 16)$

26)  $(ab + 2)(a^2b^2 - 2ab + 4)$

27) \$11.25

28) \$13.33

29) \$456.52

30) \$490.65

31) 4.2 hr

32) 2.36 hr

33)  $\frac{3}{x}$

34)  $\frac{4}{x}$

35)  $\frac{1}{5x + 2}$

36)  $\frac{1}{5x + 4}$

37)  $\frac{y + 7}{y + 8}$

## Answer Key

Testname: EXAM2PREP\_COMPRESSED\_CH4ANDCH5V01

$$38) \frac{y+2}{y+7}$$

$$39) \frac{m+5}{m-5}$$

$$40) \frac{m-8}{m+8}$$

41) 3

42) 2

43) -8, -7

44) -5, -8

45) 7, 6

46) -8, 4

47) -2, 9

48) D

49) B

50) A

51) C

52) {-8, 8}

53) {-2, 2}

54) {-2, 2}

55) {-4, 4}

56) {-2, 2}

57) {-3, 3}

58) {-3, 3}

59)  $\emptyset$

60)  $\emptyset$

61)  $\emptyset$

62) 9

63) 3

64) 2 or 6

65) 1 or 6

66) 1 or 5

67) 120 mph

68) 234 mph

69) 126 mph

70) 171 mph

$$71) \frac{-3(x+9)}{(x-4)(x-7)}$$

$$72) \frac{10(x-7)}{(x-1)(x+9)}$$

$$73) \frac{-6(x+3)}{(x+5)(x-1)}$$

$$74) \frac{-13(x-2)}{(x+8)(x-5)}$$

$$75) \frac{11x+56}{3(x+7)(x-7)}$$

$$76) \frac{7x+24}{4(x+8)(x-8)}$$

## Answer Key

Testname: EXAM2PREP\_COMPRESSED\_CH4ANDCH5V01

$$77) \frac{13x + 20}{3(x + 2)(x - 2)}$$

$$78) \frac{11x + 14}{4(x + 2)(x - 2)}$$

$$79) \frac{f}{g}(x) = \frac{x - 5}{x - 7}$$

$$80) \frac{f}{g}(x) = \frac{x - 4}{x - 8}$$

$$81) \frac{f}{g}(x) = \frac{x - 8}{x - 9}$$

$$82) \frac{f}{g}(x) = \frac{x + 4}{x - 9}$$

$$83) \frac{f}{g}(x) = \frac{x + 4}{x + 7}$$

84) Vertical:  $x = 2$ ; horizontal:  $y = -4$ ;  $(-\infty, 2) \cup (2, \infty)$

85) Vertical:  $x = 1$ ; horizontal:  $y = 4$ ;  $(-\infty, 1) \cup (1, \infty)$

86) Vertical:  $x = 2$ ; horizontal:  $y = -3$ ;  $(-\infty, 2) \cup (2, \infty)$

87) Vertical:  $x = -4$ ; horizontal:  $y = -1$ ;  $(-\infty, -4) \cup (-4, \infty)$

88) Vertical:  $x = 1$ ; horizontal:  $y = -2$ ;  $(-\infty, 1) \cup (1, \infty)$

89) Vertical:  $x = 2$ ; horizontal:  $y = 3$ ;  $(-\infty, 2) \cup (2, \infty)$