

$$\textcircled{1} \frac{4}{x+3} \cdot \frac{x-5}{9}$$

$$= \boxed{\frac{4x-20}{9x+27}}$$

$$\textcircled{3} \frac{x}{3} \cdot \frac{12}{x+5}$$

$$= \frac{x}{\cancel{3}} \cdot \frac{\cancel{3} \cdot 4}{x+5}$$

$$= \boxed{\frac{4x}{x+5}}$$

$$\textcircled{5} \frac{3}{x} \cdot \frac{4x}{15}$$

$$= \frac{\cancel{3}}{x} \cdot \frac{4x}{\cancel{3} \cdot 5}$$

$$= \boxed{\frac{4}{5}}$$

$$\textcircled{7} \frac{x-3}{x+5} \cdot \frac{4x+20}{9x-27}$$

$$= \frac{\cancel{(x-3)}}{\cancel{(x+5)}} \cdot \frac{4\cancel{(x+5)}}{9\cancel{(x-3)}}$$

$$= \boxed{\frac{4}{9}}$$

$$\textcircled{9} \frac{x^2+9x+14}{x+7} \cdot \frac{1}{x+2}$$

$$= \frac{\cancel{(x+2)}\cancel{(x+7)}}{\cancel{(x+7)}} \cdot \frac{1}{\cancel{(x+2)}}$$

$$= \boxed{1}$$

$$\textcircled{11} \frac{x^2-25}{x^2-3x-10} \cdot \frac{x+2}{x}$$

$$= \frac{\cancel{(x-5)}\cancel{(x+5)}}{\cancel{(x-5)}\cancel{(x+2)}} \cdot \frac{\cancel{(x+2)}}{x}$$

$$= \boxed{\frac{x+5}{x}}$$

$$\textcircled{13} \frac{4y+30}{y^2-3y} \cdot \frac{y-3}{2y+15}$$

$$= \frac{2\cancel{(2y+15)}}{y\cancel{(y-3)}} \cdot \frac{\cancel{(y-3)}}{\cancel{(2y+15)}}$$

$$= \boxed{\frac{2}{y}}$$

$$\textcircled{15} \frac{y^2 - 7y - 30}{y^2 - 6y - 40} \cdot \frac{2y^2 + 5y + 2}{2y^2 + 7y + 3}$$

$$= \frac{\cancel{(y-10)}(y+3)}{\cancel{(y-10)}(y+4)} \cdot \frac{\cancel{(2y+1)}(y+2)}{\cancel{(2y+1)}(y+3)}$$

$$= \boxed{\frac{y+2}{y+4}}$$

$$\textcircled{17} (y^2 - 9) \cdot \frac{4}{y-3}$$

$$= (y+3)\cancel{(y-3)} \cdot \frac{4}{\cancel{(y-3)}}$$

$$= \boxed{4(y+3)}$$

$$\textcircled{19} \frac{x^2 - 5x + 6}{x^2 - 2x - 3} \cdot \frac{x^2 - 1}{x^2 - 4}$$

$$= \frac{\cancel{(x-3)}(x-2)}{\cancel{(x-3)}(x+1)} \cdot \frac{(x-1)\cancel{(x+1)}}{\cancel{(x-2)}(x+2)}$$

$$= \boxed{\frac{x-1}{x+2}}$$

$$\textcircled{21} \frac{x^3 - 8}{x^2 - 4} \cdot \frac{x+2}{3x}$$

$$= \frac{\cancel{(x-2)}(x^2 + 2x + 4)}{\cancel{(x-2)}(x+2)} \cdot \frac{\cancel{(x+2)}}{3x}$$

$$= \boxed{\frac{x^2 + 2x + 4}{3x}}$$

$$\textcircled{23} \frac{(x-2)^3}{(x-1)^3} \cdot \frac{x^2-2x+1}{x^2-4x+4}$$

$$= \frac{\cancel{(x-2)}^2(x-2)}{\cancel{(x-1)}^2(x-1)} \cdot \frac{\cancel{(x-1)}^2}{\cancel{(x-2)}^2}$$

$$= \boxed{\frac{x-2}{x-1}}$$

$$\textcircled{25} \frac{6x+2}{x^2-1} \cdot \frac{1-x}{3x^2+x}$$

$$= \frac{2\cancel{(3x+1)}}{\cancel{(x-1)}(x+1)} \cdot \frac{-1\cancel{(x-1)}}{x\cancel{(3x+1)}}$$

$$= \boxed{\frac{-2}{x(x+1)}}$$

$$\textcircled{27} \frac{25-y^2}{y^2-2y-35} \cdot \frac{y^2-8y-20}{y^2-3y-10}$$

$$= \frac{(5-y)\cancel{(5+y)}}{(y-7)(y+5)} \cdot \frac{(y-10)\cancel{(y+2)}}{(y-5)\cancel{(y+2)}}$$

$$= \frac{-1 \cdot \cancel{(y-5)}}{(y-7)} \cdot \frac{(y-10)}{\cancel{(y-5)}}$$

$$= \boxed{\frac{-(y-10)}{y-7}}$$

or

$$= \boxed{-\frac{y-10}{y-7}}$$

$$(29) \frac{x^2 - y^2}{x} \cdot \frac{x^2 + xy}{x + y}$$

$$= \frac{(x-y)(x+y)}{x} \cdot \frac{x(x+y)}{(x+y)}$$

$$= \boxed{(x-y)(x+y)}$$

$$(31) \frac{x^2 + 2xy + y^2}{x^2 - 2xy + y^2} \cdot \frac{4x - 4y}{3x + 3y}$$

$$= \frac{(x+y)^2}{(x-y)^2} \cdot \frac{4(x-y)}{3(x+y)}$$

$$= \frac{(x+y)(x+y)}{(x-y)(x-y)} \cdot \frac{4(x-y)}{3(x+y)}$$

$$= \boxed{\frac{4(x+y)}{3(x-y)}}$$

$$(33) \frac{x}{7} \div \frac{5}{3}$$

$$= \frac{x}{7} \cdot \frac{3}{5}$$

$$= \boxed{\frac{3x}{35}}$$

$$(35) \frac{3}{x} \div \frac{12}{x}$$

$$= \frac{3}{x} \cdot \frac{x}{12}$$

$$= \frac{3}{x} \cdot \frac{1 \cdot x}{3 \cdot 4}$$

$$= \boxed{\frac{1}{4}}$$

$$(37) \frac{15}{x} \div \frac{3}{2x}$$

$$= \frac{3 \cdot 5}{x} \cdot \frac{2x}{3}$$

$$= \boxed{10}$$

$$\begin{aligned} \textcircled{39} \quad \frac{x+1}{3} &\div \frac{3x+3}{9} \\ &= \frac{\cancel{x+1}}{3} \cdot \frac{9}{3\cancel{(x+1)}} \\ &= \boxed{\frac{3}{1}} \end{aligned}$$

$$\begin{aligned} \textcircled{41} \quad \frac{7}{x-5} &\div \frac{28}{3x-15} \\ &= \frac{7}{\cancel{x-5}} \cdot \frac{3\cancel{(x-5)}}{4 \cdot 7} \\ &= \boxed{\frac{3}{4}} \end{aligned}$$

$$\begin{aligned} \textcircled{43} \quad \frac{x^2-4}{x} &\div \frac{x+2}{x-2} \\ &= \frac{(x-2)\cancel{(x+2)}}{x} \cdot \frac{\cancel{(x-2)}}{\cancel{(x+2)}} \\ &= \boxed{\frac{(x-2)^2}{x}} \end{aligned}$$

$$\begin{aligned} \textcircled{45} \quad (y^2-16) &\div \frac{y^2+3y-4}{y^2+4} \\ &= \frac{(y-4)\cancel{(y+4)}(y^2+4)}{(y-1)\cancel{(y+4)}} \\ &= \frac{(y-4)(y^2+4)}{y-1} \end{aligned}$$

$$\begin{aligned} \textcircled{47} \quad \frac{y^2-y}{15} &\div \frac{y-1}{5} \\ &= \frac{y\cancel{(y-1)}}{3 \cdot 5} \cdot \frac{5}{\cancel{(y-1)}} \\ &= \boxed{\frac{y}{3}} \end{aligned}$$

$$\begin{aligned} \textcircled{49} \quad \frac{4x^2+10}{x-3} &\div \frac{6x^2+15}{x^2-9} \\ &= \frac{2\cancel{(2x+5)}}{\cancel{(x-3)}} \cdot \frac{\cancel{(x-3)}(x+3)}{3\cancel{(2x+5)}} \\ &= \frac{2(x+3)}{3} \end{aligned}$$

$$\textcircled{51} \frac{x^2 - 25}{2x - 2} \div \frac{x^2 + 10x + 25}{x^2 + 4x - 5}$$

$$= \frac{(x-5)(x+5)}{2(x-1)} \cdot \frac{(x-1)(x+5)}{(x+5)(x+5)}$$

$$= \boxed{\frac{x-5}{2}}$$

$$\textcircled{53} \frac{y^3 + y}{y^2 - y} \div \frac{y^3 - y^2}{y^2 - 2y + 1} \quad \textcircled{55} \frac{y^2 + 5y + 4}{y^2 + 12y + 32} \div \frac{y^2 - 12y + 35}{y^2 + 3y - 40}$$

$$= \frac{y(y^2 + 1)}{y(y-1)} \cdot \frac{(y-1)(y+1)}{y^2(y-1)} = \frac{(y+1)(y+4)}{(y+4)(y+8)} \cdot \frac{(y-5)(y+8)}{(y-7)(y-5)}$$

$$= \boxed{\frac{y^2 + 1}{y}}$$

$$= \boxed{\frac{y+1}{y-7}}$$

$$\textcircled{57} \frac{2y^2 - 128}{y^2 + 16y + 64} \div \frac{y^2 - 6y - 16}{3y^2 + 30y + 48}$$

$$= \frac{2(y^2 - 64)}{(y+8)^2} \cdot \frac{3(y^2 + 10y + 16)}{(y-8)(y+2)}$$

$$= \frac{2(y-8)(y+8)}{(y+8)(y+8)} \cdot \frac{3(y+2)(y+8)}{(y-8)(y+2)}$$

$$\textcircled{p6} = \boxed{6}$$

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$$\begin{aligned} \textcircled{59} \quad \frac{2x+2y}{3} &= \frac{x^2-y^2}{x-y} & \textcircled{61} \quad x^2-y^2 &= \frac{4x-4y}{x+y} \\ &= \frac{2(x+y)}{3} \cdot \frac{(x-y)}{(x-y)(x+y)} & &= \frac{(x+y)}{4(x-y)} \\ &= \boxed{\frac{2}{3}} & &= \frac{(x+y)^2}{8(x-y)(x-y)} \end{aligned}$$

$$\begin{aligned} \textcircled{63} \quad \frac{xy-y^2}{x^2+2x+1} &= \frac{2x^2+xy-3y^2}{2x^2+5xy+3y^2} \\ &= \frac{y(x-y)}{(x+1)(x+1)} \cdot \frac{(2x+3y)(x+y)}{(x-y)(2x+3y)} \\ &= \boxed{\frac{y(x+y)}{(x+1)^2}} \end{aligned}$$

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$$\left(\frac{y-2}{y^2-9y+18} \cdot \frac{y^2-4y-12}{y+2} \right) \div \frac{y^2-4}{y^2+5y+6}$$

$$= \frac{\cancel{(y-2)}}{\cancel{(y-6)}(y-3)} \cdot \frac{\cancel{(y-6)}\cancel{(y+2)}}{\cancel{(y+2)}} \cdot \frac{\cancel{(y+2)}(y+3)}{\cancel{(y-2)}\cancel{(y+2)}}$$

$$= \boxed{\frac{y+3}{y-3}}$$