

① $2x^5 + 6x^4 + 4x^3 = 2x^3(x^2 + 3x + 2)$

Three Terms
 $2x^5, 6x^4, 4x^3$
Common Factor
 $2x^3$

③ $(A + B)^2 = \boxed{A^2 + 2AB + B^2}$

$(2x + 3)^2 = \boxed{4x^2 + 6x + 9}$

⑤ $A^2 - B^2 = (A - B)(A + B)$

$4x^2 - 25 = (2x - 5)(2x + 5)$

⑦ $x^2 - 3x + 7$ Type Trinomial Terms $x^2, -3x, 7$ Degree Two

⑨ -8 Monomial -8 Zero

⑪ $x - x^2 + x^3 - x^4$ Four Terms $x, -x^2, x^3, -x^4$ Four

⑬ $(12x - 7) - (5x - 12)$
 $= 7x + 5$

⑮ $(3x^2 + x + 1) + (2x^2 - 3x - 5)$
 $= 5x^2 - 2x - 4$

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$$(17) (x^3 + 6x^2 - 4x + 7) - (3x^2 + 2x - 4)$$

$$= \boxed{x^3 + 3x^2 - 6x + 11}$$

$$(19) 8(2x + 5) - 7(x - 9)$$

$$= 16x + 40 - 7x + 63$$

$$= \boxed{9x + 103}$$

$$(21) 2(2 - 5t) + t^2(t - 1) - (t^4 - 1)$$

$$= 4 - 10t + t^3 - t^2 - t^4 + 1$$

$$= \boxed{-t^4 + t^3 - t^2 - 10t + 5}$$

$$(23) (3t - 2)(7t - 4)$$

$$= \boxed{21t^2 - 2t + 8}$$

$$(25) (3x + 5)(2x - 1)$$

$$= \boxed{6x^2 + 7x - 5}$$

$$(27) (x + 3y)(2x - y)$$

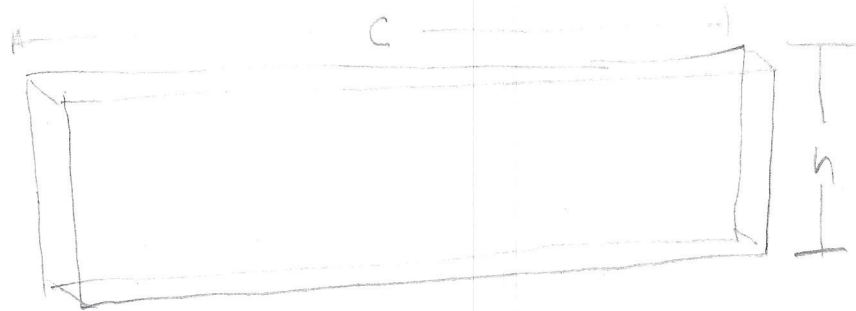
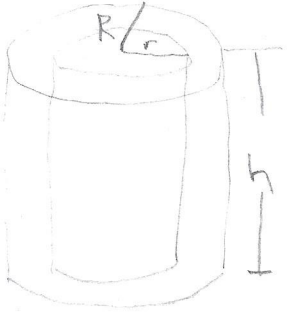
$$= \boxed{2x^2 + 5xy - 3y^2}$$

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(131)

$$V = \pi R^2 h - \pi r^2 h$$

$$V = \pi h (R^2 - r^2)$$



$$c = \frac{2\pi}{r}$$

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$$\textcircled{29} (3x+4)^2 = 9x^2 + 24x + 16$$

$$\textcircled{31} (2u+v)^2 = 4u^2 + 4uv + v^2$$

$$\textcircled{33} (2x+3y)^2 = 4x^2 + 12xy + 9y^2$$

$$\textcircled{35} (x+5)(x-5) = x^2 - 25$$

$$\textcircled{37} (3x-4)(3x+4) = 9x^2 - 16$$

$$\textcircled{39} (\sqrt{x}+2)(\sqrt{x}-2) \quad \text{note: } (\sqrt{x})(\sqrt{x}) = x$$
$$= x - 4$$

$$\textcircled{40} (\sqrt{y}+\sqrt{2})(\sqrt{y}-\sqrt{2}) = y - 2$$

$$\textcircled{41} (y+2)^3 = (y+2)(y+2)(y+2)$$
$$= (y^2 + 4y + 4)(y+2)$$
$$= y^3 + 4y^2 + 4y + 2y^2 + 8y + 8$$
$$= y^3 + 6y^2 + 12y + 8$$

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(43) $(1-2r)^3 = (1-4r+4r^2)$
 $= 4r^2 - 4r + 1$

(45) $(x+2)(x^2+2x+3)$
 $= x^3 + 2x^2 + 3x$
 $+ 2x^2 + 4x + 6$

 $= \boxed{x^3 + 4x^2 + 7x + 6}$

(47) $(2x-5)(x^2-x+1)$
 $= 2x^3 - 2x^2 + 2x$
 $+ -5x^2 + 5x - 5$

 $= \boxed{2x^3 - 7x^2 + 7x - 5}$

(50) $x^{\frac{3}{2}} \left(\sqrt{x} - \frac{1}{\sqrt{x}} \right)$
 $= x^{\frac{3}{2}} \left(x^{\frac{1}{2}} - x^{-\frac{1}{2}} \right)$

(49) $\sqrt{x}(x - \sqrt{x}) = x\sqrt{x} - x$

(51) $y^{\frac{1}{3}} \left(y^{\frac{2}{3}} + y^{\frac{5}{3}} \right) = y^{\frac{3}{3}} + y^{\frac{6}{3}}$
 $= y + y^2$
 $= \boxed{y^2 + y}$

$= x^{\frac{4}{2}} - x^{\frac{2}{2}}$
 $= x^2 - x$

(52) $x^{\frac{1}{4}} \left(2x^{\frac{3}{4}} - x^{\frac{1}{4}} \right)$
 $= 2x^{\frac{4}{4}} - x^0$
 $= 2x - 1$

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$$\textcircled{53} (x^2 - a^2)(x^2 + a^2) \\ = \boxed{x^4 - a^4}$$

$$\textcircled{54} (x^{\frac{1}{2}} + y^{\frac{1}{2}})(x^{\frac{1}{2}} - y^{\frac{1}{2}}) \\ = \boxed{x - y}$$

$$\textcircled{55} (\sqrt{a} - \sqrt{b})(\sqrt{a} + \sqrt{b}) \\ = \boxed{a - b}$$

$$\textcircled{56} (\sqrt{h^2 + 1} + 1)(\sqrt{h^2 + 1} - 1) \\ = (h^2 + 1) - 1 \\ = \boxed{h^2}$$

$$\textcircled{57} ((x-1) + x^2)((x-1) - x^2) \\ = (x-1)^2 - x^4 \\ = \boxed{x^2 - x^2 - 2x + 1}$$

$$\textcircled{58} (x + (2 + x^2))(x - (2 + x^2)) \\ = x^2 - (2 + x^2)^2 \\ = x^2 - (4 + 4x^2 + x^4) \\ = \boxed{x^4 - 3x^2 - 4}$$

$$\textcircled{59} (2x + y - 3)(2x + y + 3) \\ = (2x + y)^2 - 9 \\ = \boxed{4x^2 + 4xy + y^2 - 9}$$

$$\textcircled{60} (x + y + z)(x - y - z) \\ = [x + (y + z)][x - (y + z)] \\ = x^2 - (y + z)^2 \\ = x^2 - [y^2 + 2yz + z^2] \\ = x^2 - y^2 - 2yz + z^2$$

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$$\textcircled{61} \quad -2x^3 + 16x$$

$$= \boxed{-2x(x^2 - 8)} \text{ or } \boxed{2x(-x + 8)}$$

$$\textcircled{62} \quad 2x^4 + 4x^3 - 14x^2$$

$$= \boxed{2x^2(x^2 + 2x - 7)} \text{ or } \boxed{-2x^2(-x^2 - 2x + 7)}$$

$$\textcircled{63} \quad y(y-6) + 9(y-6)$$

$$= \boxed{(y-6)(y+9)}$$

$$\textcircled{64} \quad (z+2)^2 - 5(z+2)$$

$$= (z+2)(z+2-5)$$

$$= (z+2)(z-3)$$

$$\textcircled{65} \quad 2x^2y - 6xy^2 + 3xy$$

$$= \boxed{xy(2x - 6y + 3)}$$

$$\textcircled{66} \quad -7x^4y^2 + 14xy^3 + 21xy^4$$

$$= -7xy^2(x^3 - 2y - 3y^2)$$

$$\textcircled{67} \quad x^2 + 2x - 3$$

$$= \boxed{(x-3)(x+1)}$$

$$\textcircled{68} \quad x^2 - 6x + 5$$

$$= \boxed{(x-5)(x-1)}$$

$$\textcircled{69} \quad 8x^2 - 14x - 15$$

$$= \boxed{(2x-5)(4x+3)}$$

$$\textcircled{70} \quad 6y^2 + 11y - 21$$

$$= \boxed{(6y-7)(y+3)}$$

$$\textcircled{71} \quad 3x^2 - 16x + 5$$

$$= \boxed{(3x-1)(x-5)}$$

$$\textcircled{72} \quad 5x^2 - 7x - 6$$

$$= \boxed{(5x+3)(x-2)}$$

$$\textcircled{73} \quad (3x+2)^2 + 8(3x+2) + 12$$

$$= \boxed{[(3x+2) + 6][(3x+2) + 2]}$$

$$= \boxed{(3x+8)(3x+4)}$$

$$\textcircled{74} \quad 2(a+b)^2 + 5(a+b) - 3$$

$$= \boxed{[2(a+b) - 1][(a+b) + 3]}$$

$$= \boxed{(2a+b-1)(a+b+3)}$$

$$\textcircled{75} \quad 9a^2 - 16$$

$$= \boxed{(3a-4)(3a+4)}$$

$$\textcircled{76} \quad (x+3)^2 - 4$$

$$= \boxed{[(x+3) - 2][(x+3) + 2]}$$

$$= \boxed{(x+5)(x-1)}$$

(77) $27x^3 + y^3$
 $= (3x+y)(9x^2 - 3xy + y^2)$

(78) $a^3 - b^6$
 $= (a - b^2)(a^2 + ab^2 + b^4)$

(79) $8s^3 - 125t^3$
 $= (2s - 5t)(4s^2 + 10st + 25t^2)$

(80) $1 + 1000y^3$
 $= (1 + 10y)(1 - 10y + 100y^2)$

(81) $x^2 + 12x + 36$
 $= (x + 6)^2$

(82) $16z^2 - 24z + 9$
 $= (4z - 3)^2$

(83) $x^3 + 4x^2 + x + 4$
 $x^2(x+4) + 1(x+4)$
 $= (x+4)(x^2+1)$

(84) $3x^3 - x^2 + 6x - 2$
 $= x^2(3x-1) + 2(3x-1)$
 $= (3x-1)(x^2+2)$

(85) $2x^3 + x^2 - 6x - 3$
 $= x^2(2x+1) - 3(2x+1)$
 $= (2x+1)(x^2-3)$ or
 $= (2x+1)(x-\sqrt{3})(x+\sqrt{3})$

(86) $-9x^3 - 3x^2 + 3x + 1$
 $= -3x^2(3x+1) + 1(3x+1)$
 $= (3x+1)(-3x^2+1)$
 $= -(3x+1)(3x^2-1)$ or
 $= -(3x+1)(\sqrt{3}x-1)(\sqrt{3}x+1)$

(87) $x^3 + x^2 + x + 1$
 $x^2(x+1) + 1(x+1)$
 $= (x+1)(x^2+1)$ or

(88) $x^5 + x^4 + x + 1$
 $x^4(x+1) + 1(x+1)$
 $= (x+1)(x^4+1)$

(89) $x^{\frac{3}{2}} - x^{\frac{1}{2}}$
 $= x^{\frac{1}{2}}(x^{\frac{4}{2}} - 1)$
 $= x^{\frac{1}{2}}(x-1)(x+1)$ or
 $= \sqrt{x}(x-1)(x+1)$

(90) $3x^{-\frac{1}{2}} + 4x^{\frac{1}{2}} + x^{\frac{3}{2}}$
 $= x^{-\frac{1}{2}}(3 + 4x + x^2)$
 $= x^{-\frac{1}{2}}(x+1)(x+3)$
 $= \frac{(x+1)(x+3)}{\sqrt{x}}$

(91) $= \frac{1}{\sqrt{x}}(x+1)(x+3)$

$$\begin{aligned} \textcircled{91} \quad & x^{-\frac{3}{2}} + 2x^{-\frac{1}{2}} + x^{\frac{1}{2}} \\ &= x^{-\frac{3}{2}} (1 + 2x + x^2) \\ &= \boxed{\frac{1}{x^{\frac{3}{2}}} (1+x)^2} \text{ or} \\ &= \frac{1}{\sqrt{x^3}} (x+1)^2 \text{ or} \\ &= \frac{(x+1)^2}{\sqrt{x^3}} \text{ or } \frac{(x+1)^2}{x\sqrt{x}} \end{aligned}$$

$$\begin{aligned} \textcircled{93} \quad & (x^2+1)^{\frac{1}{2}} + 2(x^2+1)^{-\frac{1}{2}} \\ &= (x^2+1)^{-\frac{1}{2}} [(x^2+1) + 2] \\ &= (x^2+1)^{-\frac{1}{2}} (x^2+3) \\ &= \frac{1}{x^2+1} (x^2+3) \end{aligned}$$

$$\begin{aligned} \textcircled{95} \quad & 12x^3 + 18x \\ &= 6x(2x^2 + 3) \end{aligned}$$

$$\begin{aligned} \textcircled{97} \quad & x^2 - 2x - 8 \\ &= (x-4)(x+2) \end{aligned}$$

$$\begin{aligned} \textcircled{99} \quad & 2x^2 + 5x + 3 \\ &= (2x+3)(x+1) \end{aligned}$$

$$\begin{aligned} \textcircled{101} \quad & 9x^2 - 36x - 45 \\ &= 9(x^2 - 4x - 5) \\ &= 9(x-5)(x+1) \end{aligned}$$

$$\begin{aligned} \textcircled{92} \quad & (x-1)^{\frac{7}{2}} - (x-1)^{\frac{3}{2}} \\ &= (x-1)^{\frac{3}{2}} [(x-1)^2 - 1] \\ &= (x-1)^{\frac{3}{2}} [(x-1)-1][(x-1)+1] \\ &= (x-1)^{\frac{3}{2}} (x-2)(x) \end{aligned}$$

$$\begin{aligned} \textcircled{94} \quad & x^{-\frac{1}{2}} (x+1)^{\frac{1}{2}} + x^{\frac{1}{2}} (x+1)^{-\frac{1}{2}} \\ &= x^{-\frac{1}{2}} (x+1)^{-\frac{1}{2}} [(x+1) + x] \\ &= x^{-\frac{1}{2}} (x+1)^{-\frac{1}{2}} (2x+1) \\ &= \left(\frac{1}{\sqrt{x}}\right) \left(\frac{1}{\sqrt{x+1}}\right) (2x+1) \end{aligned}$$

$$\begin{aligned} \textcircled{96} \quad & 30x^3 + 15x^4 \\ &= 15x^3(2+x) \end{aligned}$$

$$\begin{aligned} \textcircled{98} \quad & x^2 - 14x + 48 \\ &= (x-8)(x-6) \end{aligned}$$

$$\begin{aligned} \textcircled{100} \quad & 2x^2 + 7x - 4 \\ &= (2x-1)(x+4) \end{aligned}$$

$$\begin{aligned} \textcircled{102} \quad & 8x^2 + 10x + 3 \\ &= (2x+1)(4x+3) \end{aligned}$$

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$$\textcircled{103} \quad 49 - 4y^2$$

$$= (7 - 2y)(7 + 2y)$$

$$\textcircled{104} \quad 4t^2 - 9s^2$$

$$= (2t - 3s)(2t + 3s)$$

$$\textcircled{105} \quad t^2 - 6t + 9$$

$$= (t - 3)^2$$

$$\textcircled{106} \quad x^2 + 10x + 25$$

$$= (x + 5)^2$$

$$\textcircled{107} \quad 4x^2 + 4xy + y^2$$

$$= (2x + y)^2$$

$$\textcircled{108} \quad r^2 - 6rs + 9s^2$$

$$= (r - 3s)^2$$

$$\textcircled{109} \quad (a + b)^2 - (a - b)^2$$

$$= [(a + b) - (a - b)][(a + b) + (a - b)]$$

$$= [2b][2a]$$

$$= 4ab$$

$$\textcircled{110} \quad \left(1 + \frac{1}{x}\right)^2 - \left(1 - \frac{1}{x}\right)^2$$

$$= \left[\left(1 + \frac{1}{x}\right) - \left(1 - \frac{1}{x}\right)\right] \left[\left(1 + \frac{1}{x}\right) + \left(1 - \frac{1}{x}\right)\right]$$

$$= \left[\frac{2}{x}\right][2]$$

$$= \frac{4}{x} \text{ or } 4\left(\frac{1}{x}\right)$$

$$\begin{aligned} (111) \quad & x^2(x^2-1) - 9(x^2-1) \\ &= (x^2-1)(x^2-9) \\ &= (x-1)(x+1)(x-3)(x+3) \end{aligned}$$

$$\begin{aligned} (112) \quad & (a^2-1)b^2 - 4(a^2-1) \\ &= (a^2-1)(b^2-4) \\ &= (a-1)(a+1)(b-2)(b+2) \end{aligned}$$

$$\begin{aligned} (113) \quad & 8x^3 - 125 \\ &= (2x-5)(4x^2+10x+25) \end{aligned}$$

$$\begin{aligned} (114) \quad & x^6 + 64 \\ &= (x^2)^3 + (4)^3 \\ &= (x^2+4)(x^4-4x^2+16) \end{aligned}$$

$$\begin{aligned} (115) \quad & x^3 + 2x^2 + x \\ &= x(x^2 + 2x + 1) \\ &= x(x+1)^2 \end{aligned}$$

$$\begin{aligned} (116) \quad & 3x^3 - 27x \\ &= 3x(x^2 - 9) \\ &= 3x(x-3)(x+3) \end{aligned}$$

$$\begin{aligned} (117) \quad & x^4y^3 - x^2y^5 \\ &= x^2y^3(x^2 - y^2) \\ &= x^2y^3(x-y)(x+y) \end{aligned}$$

$$\begin{aligned} (118) \quad & 18y^3x^2 - 2xy^4 \\ &= 2xy^3(9x - y) \end{aligned}$$

$$\begin{aligned} (119) \quad & 2x^3 + 4x^2 + x + 2 \\ &= 2x^2(x+2) + 1(x+2) \\ &= (x+2)(2x^2+1) \end{aligned}$$

$$\begin{aligned} (120) \quad & 3x^3 + 5x^2 - 6x - 10 \\ &= x^2(3x+5) - 2(3x+5) \\ &= (3x+5)(x^2-2) \end{aligned}$$

$$\begin{aligned} (121) \quad & (x-1)(x+2)^2 - (x-1)^2(x+2) \\ &= (x-1)(x+2) \left[(x+2) - (x-1) \right] \\ &= (x-1)(x+2)(3) \\ &= 3(x-1)(x+2) \end{aligned}$$

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$$\begin{aligned}
(122) \quad & y^4(y+2)^3 + y^5(y+2)^4 \\
&= y^4(y+2)^3 [1 + y(y+2)] \\
&= y^4(y+2)^3 [1 + y^2 + 2y] \\
&= y^4(y+2)^3 [y^2 + 2y + 1] \\
&= y^4(y+2)^3 (y+1)^2
\end{aligned}$$

$$\begin{aligned}
(123) \quad & (a^2+1)^2 - 7(a^2+1) + 10 \\
&= [(a^2+1) - 2] [(a^2+1) - 5] \\
&= [a^2 - 1] [a^2 - 4] \\
&= (a-1)(a+1)(a-2)(a+2)
\end{aligned}$$

$$\begin{aligned}
(124) \quad & (a^2+2a)^2 - 2(a^2+2a) - 3 \\
&= [(a^2+2a) + 1] [(a^2+2a) - 3] \\
&= [a^2+2a+1] [a^2+2a-3] \\
&= (a+1)^2(a-1)(a+3)
\end{aligned}$$

125 $5(x^2+4)^4(2x)(x-2)^4 + (x^2+4)^5(4)(x-2)^3$

$$= (x^2+4)^4(2)(x-2)^3 [5x(x-2) + (x^2+4)(2)]$$

$$= 2(x^2+4)^4(x-2)^3(5x^2 - 10x + 2x^2 + 8)$$

$$= \boxed{2(x^2+4)^4(x-2)^3(7x^2 - 10x + 8)}$$

126 ~~$3(2x-1)^2(2)(x+3)^{\frac{1}{2}} + (2x-1)^3(\frac{1}{2})(x+3)^{-\frac{1}{2}}$~~

~~$$= \frac{1}{2}(2x-1)^2(x+3)^{-\frac{1}{2}} [12(2x-1)(x+3) + 1]$$~~

~~$$= \frac{1}{2}(2x-1)^2(x+3)^{-\frac{1}{2}} (12(2x^2 + 6x - x - 3) + 1)$$~~

~~$$= \frac{1}{2}(2x-1)^2(x+3)^{-\frac{1}{2}} (24x^2 + 60x - 35)$$~~

126 $3(2x-1)^2(2)(x+3)^{\frac{1}{2}} + (2x-1)^3(\frac{1}{2})(x+3)^{-\frac{1}{2}}$

$$= \frac{1}{2}(2x-1)^2(x+3)^{-\frac{1}{2}} [(3)(4)(x+3) + (2x-1)]$$

$$= \frac{1}{2}(2x-1)^2(x+3)^{-\frac{1}{2}} [12(x+3) + 2x-1]$$

$$= \frac{(2x-1)^2}{2(x+3)^{\frac{1}{2}}} [12x + 36 + 2x - 1]$$

$$= \frac{(2x-1)^2(14x+35)}{2\sqrt{x+3}}$$

$$= \boxed{\frac{(2x-1)^2(14x+35)}{2\sqrt{x+3}}}$$

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$$\begin{aligned}
 & \textcircled{127} (x^2+3)^{-\frac{1}{3}} - \frac{2}{3}x^2(x^2+3)^{-\frac{4}{3}} \\
 &= (x^2+3)^{-\frac{4}{3}} \left[(x^2+3) - \frac{2}{3}x^2 \right] \\
 &= (x^2+3)^{-\frac{4}{3}} \left(\frac{1}{3}x^2+3 \right) \\
 &= (x^2+3)^{-\frac{4}{3}} \left(\frac{1}{3} \right) (x^2+1) \\
 &= \frac{(x^2+1)}{3(x^2+3)^{\frac{4}{3}}}
 \end{aligned}$$

$$\textcircled{128} \frac{1}{2}x^{-\frac{1}{2}}(3x+4)^{\frac{1}{2}} - \frac{3}{2}x^{\frac{1}{2}}(3x+4)^{-\frac{1}{2}}$$

$$= \frac{1}{2}x^{-\frac{1}{2}}(3x+4)^{-\frac{1}{2}} \left[(3x+4) - 3x \right]$$

$$= \frac{1}{2} \left(x^{-\frac{1}{2}} \right) (3x+4)^{\frac{1}{2}} (4)$$

$$= 2 \left(x^{-\frac{1}{2}} \right) (3x+4)^{\frac{1}{2}}$$

or

$$= \frac{2}{x^{\frac{1}{2}}(3x+4)^{\frac{1}{2}}}$$