

p. 260
3.4

⑤ $P(x) = x^3 - 4x^2 + 3$

$\frac{\pm 1}{\pm 1}$ or $\frac{\pm 3}{\pm 1} = \pm 1$ or ± 3

possible rational zeros of P
Factor of constant term

factor of leading coefficient

$\frac{\pm 1, \pm 3}{\pm 1}$

 $\pm 1, \pm 2, \pm 4, \pm 8$

 ± 1

⑥ $Q(x) = x^4 - 3x^3 - 6x + 8$

possible rational zeros of Q

$\frac{P}{Q}$ $\frac{\text{Factors of constant}}{\text{factors of leading coefficient}}$

$\pm 1, \pm 2, \pm 4, \pm 8$

⑦ $R(x) = 2x^5 + 3x^3 + 4x^2 - 8$

possible rational zeros of R

$\frac{P}{Q}$ $\frac{\text{Factors of constant}}{\text{factors of leading coefficient}}$

$\frac{\pm 1, \pm 2, \pm 4, \pm 8}{\pm 1, \pm 2}$

$\pm 1, \pm 2, \pm 4, \pm 8, \pm \frac{1}{2}$

⑧ $S(x) = 6x^4 - x^2 + 2x + 12$

Possible Rational zeros of S

$\frac{P}{Q}$ $\frac{\text{Factors of constant}}{\text{Factors of Leading Coefficient}}$

$\frac{\pm 1, \pm 2, \pm 3, \pm 4, \pm 6, \pm 12}{\pm 1, \pm 2, \pm 3, \pm 6}$

$\pm 1, \pm 2, \pm 3, \pm 4, \pm 6, \pm 12$
 $\pm \frac{1}{2}, \pm \frac{3}{2}$
 $\pm \frac{1}{3}, \pm \frac{2}{3}, \pm \frac{4}{3}$

 $\pm \frac{1}{6}$

9) $T(x) = 4x^4 - 2x^2 - 7$

Rational ^{zero} Factors of T are

$$\frac{p}{q} \quad \frac{\text{Factors of constant term}}{\text{Factors of leading coefficient}} \quad \frac{\pm 1, \pm 7}{\pm 1, \pm 2, \pm 4}$$

$$\begin{aligned} &\pm 1, \pm 7 \\ &\pm \frac{1}{2}, \pm \frac{7}{2} \\ &\pm \frac{1}{4}, \pm \frac{7}{4} \end{aligned}$$

10) $U(x) = 12x^5 + 6x^3 - 2x - 8$

Possible Rational ^{zero} Factors of U

$$\frac{p}{q} \quad \frac{\text{Factors of constant}}{\text{Factors of leading coefficient}} \quad \frac{\pm 1, \pm 2, \pm 4, \pm 8}{\pm 1, \pm 2, \pm 3, \pm 4, \pm 6, \pm 12}$$

$$\begin{aligned} &\pm 1, \pm 2, \pm 4, \pm 8 \\ &\pm \frac{1}{2}, \text{ Duplicates} \\ &\pm \frac{1}{3}, \pm \frac{2}{3}, \pm \frac{4}{3}, \pm \frac{8}{3} \\ &\pm \frac{1}{4}, \text{ Duplicates} \\ &\pm \frac{1}{6}, \text{ Duplicates} \\ &\pm \frac{1}{12} \end{aligned}$$

11

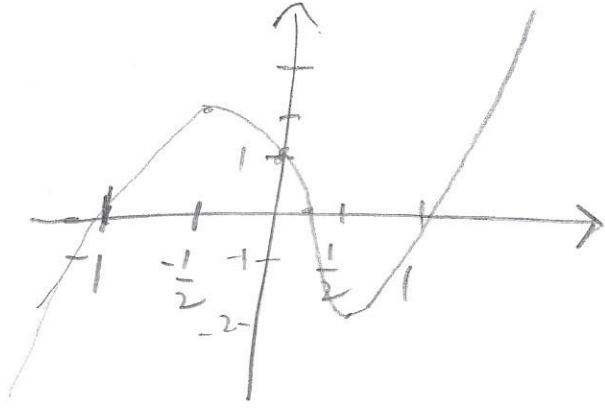
$$P(x) = 5x^3 - x^2 - 5x + 1$$

Possible rational zeros of P

$\frac{p}{q}$	constant factors	± 1
	Leading coefficient factors	$\pm 1, \pm 5$

a) $\pm 1, \pm \frac{1}{5}$

b) $-1, \frac{1}{5}, 1$



15) $x^3 + 3x^2 - 4 = P(x)$

possible zero factors of P

$\frac{p}{q}$	Factors of a_0	$\pm 1, \pm 4$
	Factor of a_n	± 1
<u>possible</u>		
$\pm 1, \pm 4$		

$P(x)$ has one variation in sign

$P(-x) = -x^3 + 3x^2 - 4$ has two variations in sign

\therefore one pos zero & two neg zeros

1 | 1 3 0 -4
 1 | 1 3 0 -4

 1 4 4 0
 1 is a factor

-1 | 1 3 0 -4 NOT
 -1 | 1 3 0 -4

 1 2 -2 -2

4 | 1 3 0 -4 NOT
 4 | 1 3 0 -4

 1 7 28

-4 | 1 3 0 -4 NOT
 -4 | 1 3 0 -4

 1 -1 4 -20

2 | 1 3 0 -4 NOT
 2 | 1 3 0 -4

 1 5 5 -6

-2 | 1 3 0 -4
 -2 | 1 3 0 -4

 1 1 -2 0 Yes

$P(x) = (x-1)(x+2)^2$



P260
3.4
17

$P(x) = x^3 - 3x - 2$ one pos factor

$P(-x) = -x^3 + 3x - 2$ two neg factors + zero

$\frac{p}{q} = \frac{\pm 1, \pm 2}{\pm 1}$

$\pm 1, \pm 2$

1 $\begin{array}{r} 1 \ 0 \ -3 \ -2 \\ \underline{1 \ 1 \ 1 \ -2} \\ 1 \ 1 \ -2 \ -4 \text{ NO} \end{array}$

-1 $\begin{array}{r} 1 \ 0 \ -3 \ -2 \\ \underline{-1 \ 1 \ 2} \\ 1 \ -1 \ -2 \ 0 \text{ Factor} \end{array}$

2 $\begin{array}{r} 1 \ 0 \ -3 \ -2 \\ \underline{2 \ 4 \ 2} \\ 1 \ 2 \ 1 \ 0 \text{ Factor} \end{array}$

-2 $\begin{array}{r} 1 \ 0 \ -3 \ -2 \\ \underline{-2 \ 4 \ -2} \\ 1 \ -2 \ 1 \ -4 \text{ NO} \end{array}$

$P(x) = (x-2)(x+1)^2$

19

$P(x) = x^3 - 6x^2 + 12x - 8$ three sign changes 3 or 1

$P(-x) = -x^3 + 6x^2 - 12x + 8$ two sign changes 2 or 0

$\frac{p}{q} = \frac{\pm 1, \pm 2, \pm 4, \pm 8}{\pm 1}$

$\pm 1, \pm 2, \pm 4, \pm 8$

$P(x) = (x-2)^3$

1 $\begin{array}{r} 1 \ -6 \ 12 \ -8 \\ \underline{1 \ 1 \ -5 \ 7} \\ 1 \ -5 \ 7 \ \text{NO} \end{array}$

-1 $\begin{array}{r} 1 \ -6 \ 12 \ -8 \\ \underline{-1 \ 7 \ -19} \\ 1 \ -7 \ 19 \ \text{NO} \end{array}$

2 $\begin{array}{r} 1 \ -6 \ 12 \ -8 \\ \underline{2 \ -8 \ 8} \\ 1 \ -4 \ 4 \ 0 \ \text{Yes} \end{array}$

-2 $\begin{array}{r} 1 \ -6 \ 12 \ -8 \\ \underline{-2 \ 16 \ -8} \\ 1 \ -8 \ 20 \ \text{NO} \end{array}$

4 $\begin{array}{r} 1 \ -6 \ 12 \ -8 \\ \underline{4 \ -8 \ 8} \\ 1 \ -2 \ -4 \ \text{NO} \end{array}$

-4 $\begin{array}{r} 1 \ -6 \ 12 \ -8 \\ \underline{-4 \ 16 \ -8} \\ 1 \ -10 \ 52 \ \text{NO} \end{array}$

8 $\begin{array}{r} 1 \ -6 \ 12 \ -8 \\ \underline{8 \ 16} \\ 1 \ -2 \ 28 \ \text{NO} \end{array}$

-8 $\begin{array}{r} 1 \ -6 \ 12 \ -8 \\ \underline{-8 \ 48 \ -8} \\ 1 \ -14 \ 40 \ \text{NO} \end{array}$

$P(x) = (x-2)^3$